Pa Longitudina man "ials PS PE]. Wood Epo LG Rigid polymer Leather foams EDUPACK EVA Pol one Neop Materials Selection – Case Study 2 las Advance Properties and Concepts

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Outline

- Case Study 13: Load-limited design, Energy-limited design and Deflection-limited design
- Case Study 14: Safe Pressure Vessels
- Multiple constraints
- Case Study 14': Light pressure Vessels with MULTIPLE CONSTRAINT APPROACH

Theory: Method of the weight factor Theory: Enhanced Digital Logic (EDL)

- Case Study 15: Precision devices
- Case Study 16: Long Span Transmission line
- Case Study 17: Light Cable
- Case Study 18: Kiln Walls
- Case Study 19: Insulation for <u>Short-Term</u> isothermal containers
- Case Study 20: Process for a Can

Secret slides : Kubota case



The Fracture-limited design



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The Fracture-limited design

The resistance of a material to the propagation of a crack is measured by its plane-strain fracture toughness value (K_{1c})

When a brittle material is deformed, it deflects elastically until it fractures. The stress at which this happens is:

$$\sigma_f = \frac{K_{1c} \cdot C}{\sqrt{\pi \cdot a_c}}$$

<u>σ_f by definition,</u> <u>To consider all the stresses</u>

		Objective	Minimize the volume	e (mass, cost)
		Constraints	Design energy specif	fied
Case Study 13:	── →	Free Variables	Choice of material	
Energy-limited design	_			the is
$\sigma_{f} = \frac{K_{1c} \cdot C}{\sqrt{\pi \cdot a_{c}}}$ $W_{el} = \frac{\sigma_{y}^{2}}{2E}$		Springs	Containment systems for turbines	Flywheels
Elastic energy	W^{r}	$^{max} = \frac{C^2}{2\pi a_c} \cdot \frac{K_{1c}}{E}$	2	
$M_2 = \frac{K_{1c}^2}{E} \approx G_c$	Toughness for a given f	flaw size	$W^{max} \qquad \frac{K_{1c}^2}{E}$	

Ductile-Brittle Temperature

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Metals, composites and some polymers $J_c > 1 \text{ kJ/m}^2$

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	Objective	Minimize the volume (mass, cost)
	Constraints	Design deflection specified
Case Study 13:	➤ Free Variables	Choice of material
Deflection-limited design		

$$\sigma_{f} = \frac{K_{1c} \cdot C}{\sqrt{\pi \cdot a_{c}}}$$
$$W_{el} = \frac{\sigma_{y}^{2}}{2E}$$
$$\varepsilon = \frac{\sigma}{E}$$

Snap on bottle tops

Snap-together fasteners

We want a large failure strain

$$\varepsilon_f = \frac{C}{\sqrt{\pi a_c}} \cdot \frac{K_{1c}}{E}$$

$$M_2 = \frac{K_{1c}}{E}$$

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Polymers, elastomers and toughest metals $\frac{K_{1c}}{E} > 10^{-3} \text{ m}^{1/2}$

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The Fracture-limited design

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No failure, but distortion Small vessels are designed to allow general yield

		Objective	•	Maximize safety (YBB)
		Constraints	•	R radius specified
Case Study 14:		Free Variables	•	Choice of material
Safe Pressure Vessels				

$$\sigma \leq \frac{C \cdot K_{1c}}{\sqrt{\pi \cdot a^*_{c}}}$$
$$\sigma = \frac{p \cdot R}{2t}$$

YBB

 $p \leq \frac{2t \cdot K_{1c}}{R \cdot \sqrt{\pi \cdot a^*_c}}$ $p \quad K_{1c} \quad But not$ Fail-safe
If the inspection is faulty for some
reasons the crack length is greater

Since
$$t = \frac{p \cdot R}{2\sigma}$$

For Thinner t

Case Study 14: Safe Pressure Vessels YBB

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Case Study 14:
Safe Pressure Vessels
LBB

$$Hp: \quad b=\frac{t}{2}$$

$$\sigma \leq \frac{C \cdot K_{1c}}{\sqrt{\pi \cdot t/2}}$$

$$\sigma_y = \frac{p \cdot R}{2t} \longrightarrow t = \frac{p \cdot R}{2\sigma_y}$$

$$p \leq \frac{4C^2}{\pi R} \cdot \left(\frac{K_{1c}^2}{\sigma_y}\right) \qquad M_2 = \frac{K_{1c}^2}{\sigma_y}$$

 a_c Tolerable crack size

$$t = \frac{p \cdot R}{2\sigma_y} \quad Thinner \ t$$

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Multiple constraints

Minimize the mass

Minimize the volume

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Case Study 14': Materials for Light pressure Vessels With MULTIPLE CONSTRAINT APPROACH

Fracture constraint

$$\int_{\alpha} \sigma = \frac{p \cdot R}{2t} \le \frac{K_{1c}}{\sqrt{\pi \cdot c}} \qquad m_1 = 2\pi R^3 \cdot p \cdot \sqrt{\pi \cdot c} \cdot \frac{\rho}{K_{1c}} \qquad M_1 = \frac{\rho}{K_{1c}}$$

$$m = 4\pi R^2 \cdot t \cdot \rho$$

$$\int_{\alpha} \text{Yield constraint}$$

$$\sigma = \frac{p \cdot R}{2t} \le \sigma_y \qquad m_2 = 2\pi R^3 \cdot p \cdot \frac{\rho}{\sigma_y} \qquad M_2 = \frac{\rho}{\sigma_y}$$

Constraints

Performance equation

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1000

Density / Yield strength (elastic limit)

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Case Study 14': Materials for Light pressure Vessels With MULTIPLE CONSTRAINT APPROACH

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$$Z_p = \alpha_H \cdot \frac{\mathrm{H}}{\mathrm{max(\mathrm{H})}} + \alpha_M \cdot \frac{\mathrm{M}}{\mathrm{max(\mathrm{M})}}$$

The most important point is to understand if you must maximize or minimize a property Example:

	Young's Modulus	Density
Maximize	E	1/ ho
Minimize	1/E	ρ

With the normalization and the performance function you can consider all the properties that you want and with various order of magnitude. But the importance coefficients? \rightarrow EDL

Example of its application

7.6. EDL method and Performance function

The performance function is a selection method to analyze different materials and to discover which is the most proper for a particular utilization; the function can correlate many different material properties and based on the requirements it is possible assign an importance sequence with the EDL (Enhanced Digital Logic). In the study this methods were utilized to correlate the hardness values and the Magnegage values. The first is a complex value to understand because is due to the matrix and to the carbide present; instead the second is a value difficult to correlate due to the precise surveys and to the empiric bases of the analyses. In a HSS a property that is consider fundamental is the low percentage of retained austenite, thus the druction is based on this assumption; as importance sign (a) the EDL method assigns 0.33 for the hardness and 0.67 for the retained austenite. The performance function is:

$$Z_p = \alpha_H \cdot \frac{H}{\max(H)} + \alpha_M \cdot \frac{M}{\max(H)}$$
(5)

Equation 5 : Performance function of the thermal treatments.

H and M are the sample values and they are divided for the maximum between them; with this important step the values are normalized, as consequence they can be correlated with other different properties and properties as Magnegage analysis can have a higher import. In the Table 33 all the performance function results (Z₂) are reported in the two relevant depths; to arrive at those values the data from Table 29 and Table 30 were used.

	R1	NO	N1	N2	NB	N4	N5	X1/X3	N6
20	0,25	0,44	0,75	0,97	0,93	0,91	0,97	0,89	0,80
50	0,54	0,47	0,68	0,80	0,78	0,80	0,91	0,92	0,77
Table 33	· Results of th	ne nerforman	ce function						

The samples are reported in order from the R1 (different thermal treatment) and N0 (as-cast conditions) to N6 that has the higher temperature of thermal treatment (double tempering). The results are putted in order from the higher value to the lower one in the two depths as shown in the Table 34.

Table 34 : The results of Table 33 in order from the highest value to the lowest for the two depths (A and B). The different sample are written together with the thermal treatment temperature. The mean values of the two depths for every sample in (C).

The best material and in this case the best thermal treatment that can be applied on the material is the double tempering in the range of temperature 525-530°C as reported in the following table; to arrive at this conclusion it was done the mean value of the two depth values to try to consider the entire roll and not only a single part of it.

Theory: Enhanced Digital Logic

$$Z_p = \alpha_H \cdot \frac{\mathrm{H}}{\mathrm{max}(\mathrm{H})} + \alpha_M \cdot \frac{\mathrm{M}}{\mathrm{max}(\mathrm{M})}$$

3-1

2-1

1-1

σ	lield Strength
W	Weldability

C Corrosion Resistance **F** Fatigue Resistance

A really more important than B	
A more important than B	
A as imp. as B	

Importan	ce Sequence
$\sigma > W$	C > F

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Theory: Enhanced Digital Logic

And if I want to have a property value similar to another material? → Normalisation MANCINI-MAURIZI

Example : Coefficient of thermal expansion α (CTE)

If the property is bigger than the target value $N_n = 1 - \frac{CTE_n - CTE_{targ.}}{CTE_{max} - CTE_{targ.}}$

If the property is smaller than the target value $N_n = 1 - \frac{CTE_{targ.} - CTE_n}{CTE_{targ.} - CTE_{min}}$

Again, a value close to 1 = the two CTEs are similar (the contrary to 0)

Using materials at high temperatures

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	Objective	Minimize distortion to maximize positional accuracy
Case Study 15: →	Constraints	Tolerate heat fluxTolerate vibration
	Free Variables	Choice of material

Es. Sub micrometer displacement gauge

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Case Study 15: Materials for Precision devices

Fourier's Law in steady state $q = -\lambda \frac{dT}{dx}$ $\varepsilon = \alpha (T - T_0)$ $\begin{array}{c} q \; \textit{Heat flux} \\ \lambda \; \textit{Thermal conductivity} \\ \frac{dT}{dx} \; \textit{resulting temperature gradient} \end{array}$

The distortion is proportional to the gradient of strain $\frac{d\varepsilon}{dx} = \alpha \cdot \frac{dT}{dx} = = \frac{\alpha}{\lambda} \cdot q$

Moreover, we want to avoid flexural vibrations at lowest frequencies; proportional to (finally must be stiff) \rightarrow

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V

Carbides? \rightarrow Excellent performances, but difficult to shape Copper \rightarrow High density gives a low M2 Al alloys \rightarrow the cheapest and most easily shaped choice Silicon \rightarrow the best choice

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With some researches you can find better materials! Ex. Invar Add Record IF IT HAS A SENSE

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Conductors, insulators and dielectrics

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	Objective	Maximize current flux
	Constraints	Easy to manufacture
Case Study 16:	•	Must be strong?
Materials for		Dimensions fixed
Long Span Transmission line	Free Variables	Choice of material

Index from General Knowledge

Case Study 16: Materials for Long Span Transmission line

Wiedemann-Franz Law $L \propto K = \frac{\lambda}{\rho_e}$

 $L \ Lorenz \ number$ K Electrical conductivity λ Thermal conductivity ρ_e electrical resistivity

$$K \uparrow \frac{\lambda}{\rho_e}$$

[http://hyperphysics.phy-astr.gsu.edu/hbase/thermo/thercond.html]

Index from « Equations »

Case Study 17: Materials for Light Cable

Pouillet's Law $r = \rho_e \frac{L}{A} \longrightarrow A = \rho_e \frac{L}{r}$ $m = \rho \cdot L \cdot A$ $m = (\rho \cdot \rho_e) \cdot \frac{L^2}{r}$

http://toelatingsexamen.org/en/app/course/71/pouillets-law-electrodynamics?chapterID=84§ionID=3

V

Case Study 18: Materials for Kiln Walls

Objective	•	Minimize energy consumed in firing cycle
Constraints	•	Maximum and minimum operating temperature Possible limit on W for space reasons
Free Variables	•	Choice of material

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Case Study 18: Materials for Kiln Walls

Heat loss by conduction

$$Q_1 = -\lambda \frac{(T_i - T_0)}{w} \cdot t$$

Heat (loss) absorbed by walls

$$Q_2 = \frac{\Delta T \cdot w \cdot \rho \cdot C_p}{2}$$

$$\begin{array}{c|c} t = 0 & T_{0} \\ t > 0 & T_{0+i} \\ \hline q. & = \text{Heat flux} \\ \lambda = \text{Thermal conductivity} \\ T_{i} & W & t = \text{time} \end{array}$$

Energy-efficient kiln walls? Reduce λ and w

Total energy consumed during the use $Q = Q_1 + Q_2$

Thus, we want a Minimum
$$Q(w) \rightarrow a$$
 w that correspond to $\frac{dQ}{dw} = 0$

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Case Study 19: Materials for Insulation for <u>Short-Term</u> isothermal containers

Fick's Law for the temperature at Steady state

$$q^{\cdot} = -\lambda \frac{(T_i - T_0)}{w}$$

Fick's Law for the temperature at not-steady state

WE ARE NOT MINIMIZING THE HEAT FLUX!!! WE WANT TO MAXIMIZE THE TIME t BEFORE T₀ CHANGE CONSIDERABLY

$$\frac{\partial T}{\partial t} = a \frac{\partial^2 T}{\partial x^2}$$
Too complex, so
we use
$$x \cong \sqrt{2at} \le w$$

$$t = \frac{w^2}{2a}$$

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	Objective	 Find an High production + Cheap process 		
Case Study 20: Process for a Can	Constraints	 Shape : Dished Sheet Physical aspect : Mass range max 1 kg Tolerance 0,2-0,5 mm Primary Process 		
	Free Variables	Choice of process		

Materials Selection

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a Study 20.	Properties Close	
e Study 20:	Link Record	Number Passed
cess for a can	MaterialUniverse: \ Metals and alloys	92 Show
		Stage Title: [MaterialUniverse:\Metals and alloys] Trees ProcessUniverse Insert ProcessUniverse Shaping Choose records from the ProcessUniverse tree. The chosen records will pass the selection. OK Cancel Help

Case Study 20: Process for a Can

Dished sheet, Mass	s range,	Tolerance	, Secondary	shaping	processes
Properties Apply	Clear				
Click on the headings to show	v/hide select	tion criteria			
▼ Shape					
Circular prismatic					
Non-circular prismatic					
Flat sheet					
Dished sheet	\checkmark				
Solid 3-D					
Hollow 3-D					
 Physical attributes 					
	Minin	num N	1aximum		
Mass range			1	kg	
Range of section thickness				mm	
Tolerance	0,2),5	mm	
Roughness				μm	
Cutting speed				m/s	
Minimum cut width				mm	
 Process characteristics 					
Primary shaping processes					
Secondary shaping processes	✓				
Machining processes					
Cutting processes					
Prototyping					
Discrete					
Continuous					

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Case Study 20: Process for a Can

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Results : **Deep drawing** (deep drawing is a particular stamping)

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Deep drawing (deep drawing is a particular stamping)

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